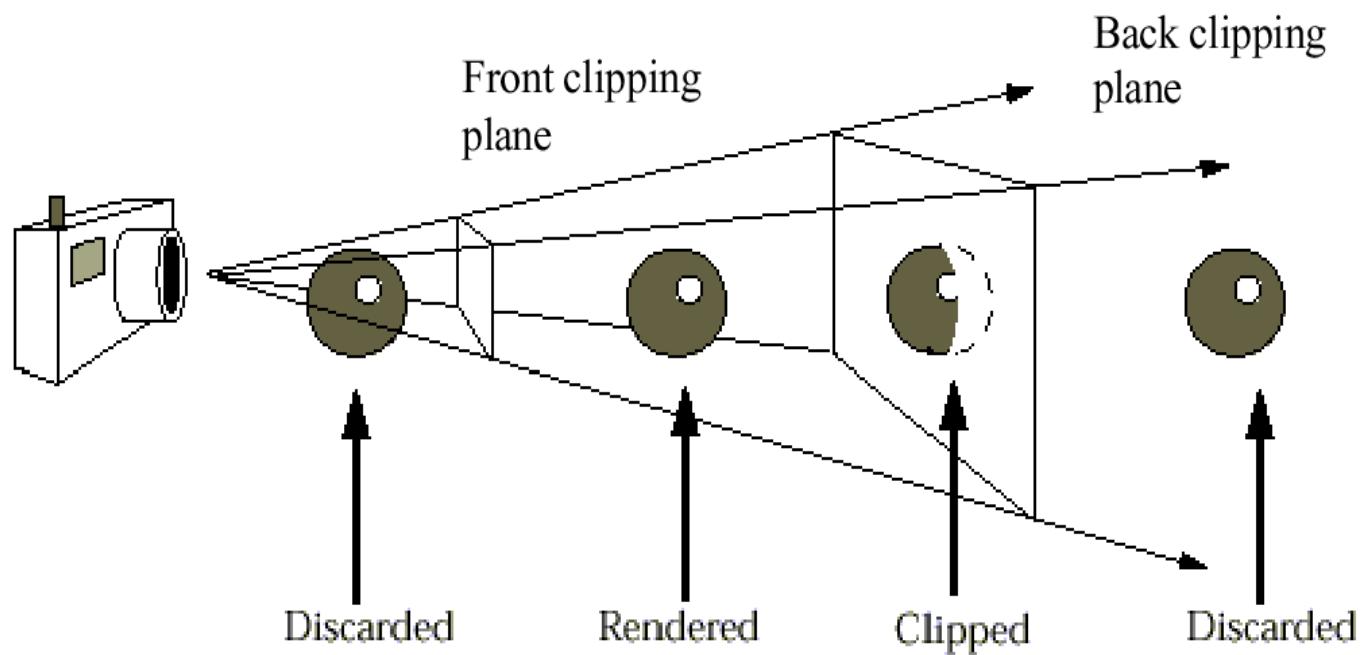
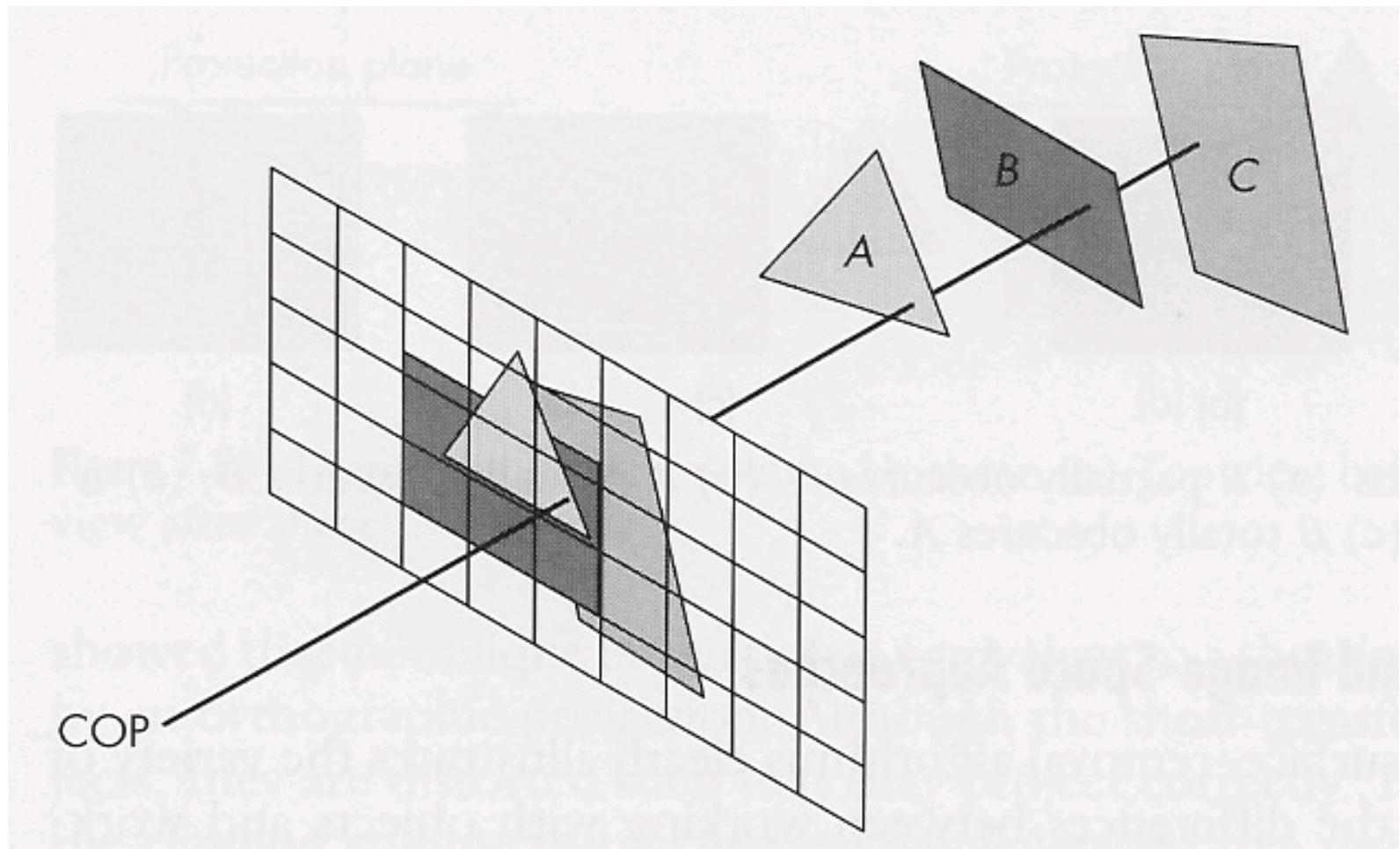


# 3D Culling and Clipping



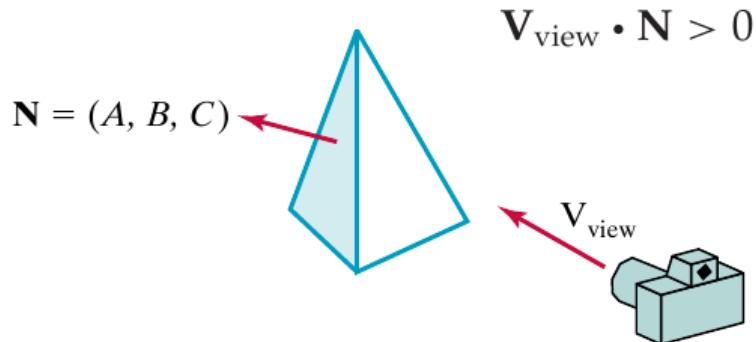
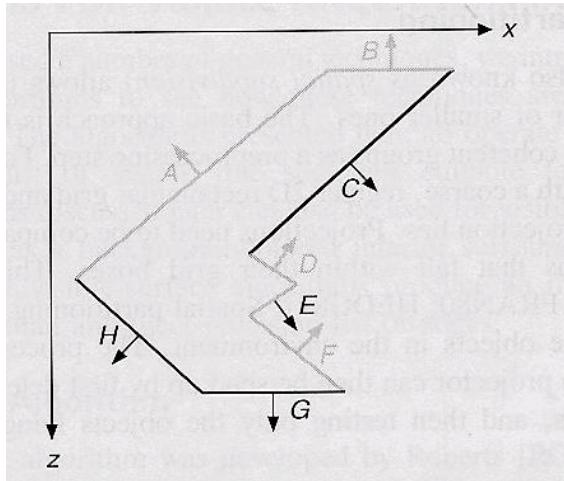
# Hidden Surface Elimination



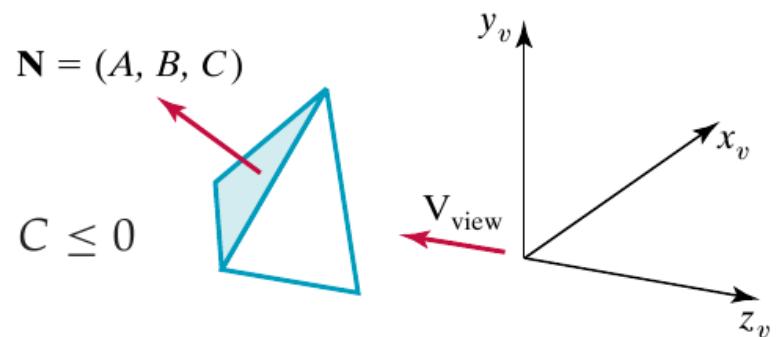
# Popular Algorithms

- Back-Face Culling
- Z-Buffer (Depth-Buffer) Algorithm
  - Frame Buffer (Color Buffer) 와
  - Z-Buffer (Depth-Buffer) 를 사용
- BSP Tree 알고리즘  
(BSP: Binary Space Partitioning)

# Back-Face Detection

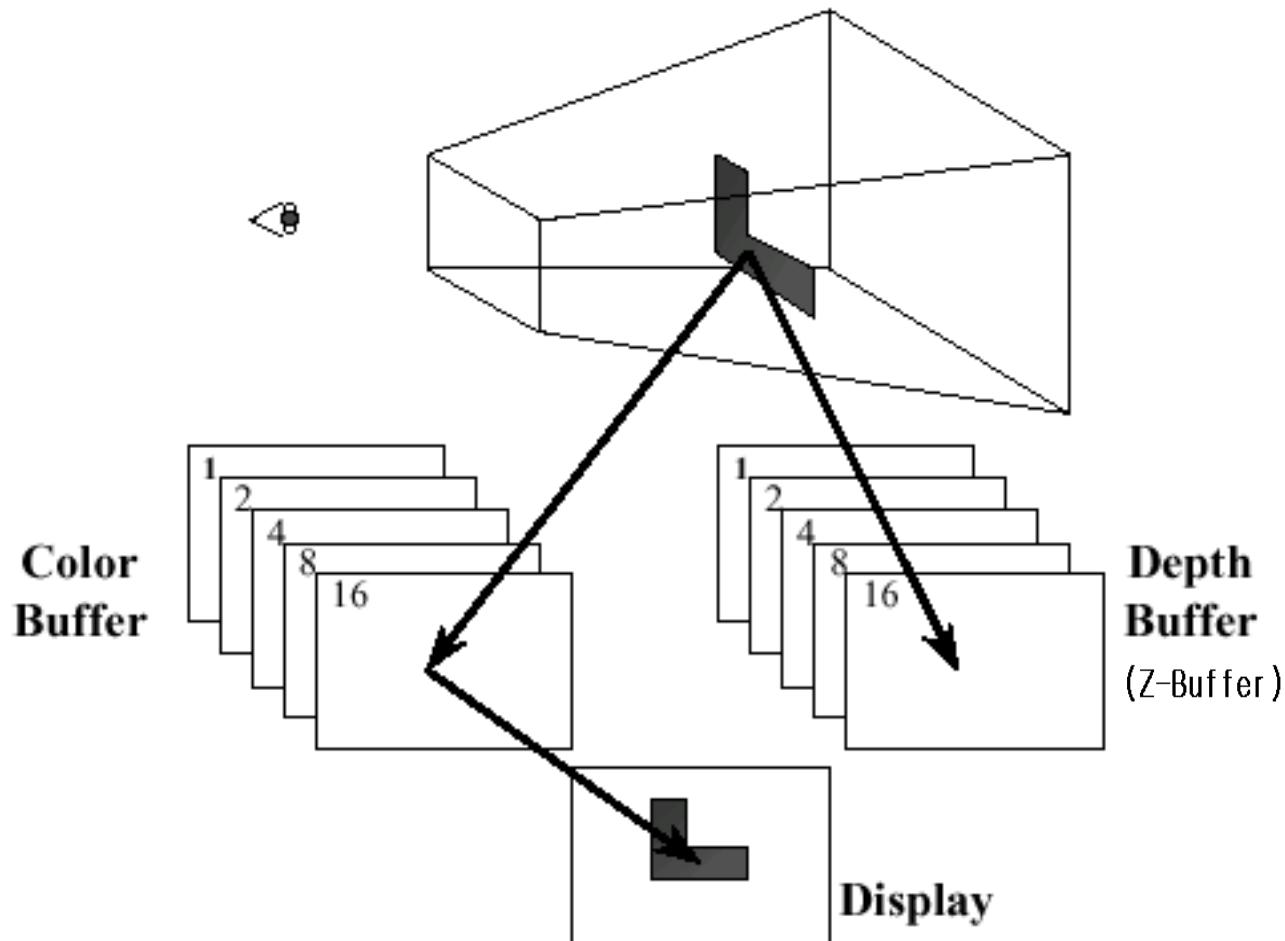


**FIGURE 9-1** A surface normal vector  $\mathbf{N}$  and the viewing-direction vector  $\mathbf{V}_{\text{view}}$ .



**FIGURE 9-2** A polygon surface with plane parameter  $C < 0$  in a right-handed viewing coordinate system is identified as a back face when the viewing direction is along the negative  $z_v$  axis.

# Color Buffer and Depth Buffer



## Depth-Buffer Algorithm

1. Initialize the depth buffer and frame buffer so that for all buffer positions  $(x, y)$ ,

```
depthBuff (x, y) = 1.0,      frameBuff (x, y) = backgndColor
```

2. Process each polygon in a scene, one at a time.

- For each projected  $(x, y)$  pixel position of a polygon, calculate the depth  $z$  (if not already known).
- If  $z < \text{depthBuff} (x, y)$ , compute the surface color at that position and set

```
depthBuff (x, y) = z,      frameBuff (x, y) = surfColor (x, y)
```

After all surfaces have been processed, the depth buffer contains depth values for the visible surfaces and the frame buffer contains the corresponding color values for those surfaces.

# Z-Buffer Algorithm



b: background color  
s: square's color

frame buffer

**z-buffer**

# Z-Buffer Algorithm



A large grid of the character 't' is arranged in a triangular pattern. The grid is bounded by a thick black border. A single 't' character is highlighted with a red box. A black line extends from the bottom right corner of the red box upwards and to the left, ending at the top vertex of the triangle.

b : background color  
S : square's color  
T : triangle's color

frame buffer

## **z-buffer**

# Depth Computation for Planes

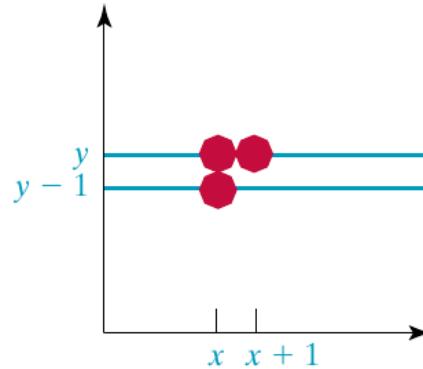
$$z = \frac{-Ax - By - D}{C}$$

$$z' = \frac{-A(x + 1) - By - D}{C}$$

$$z' = z - \frac{A}{C}$$

$$x' = x - \frac{1}{m}$$

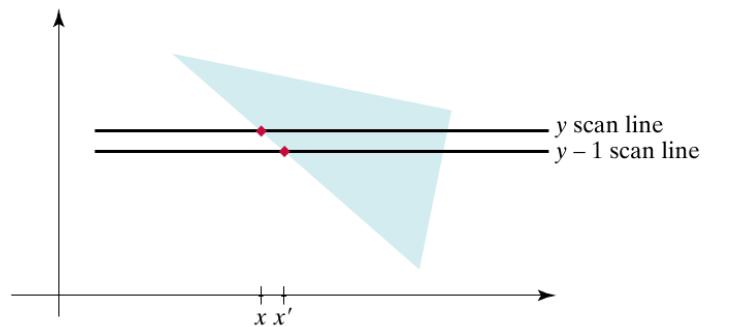
$$z' = z + \frac{A/m + B}{C}$$



**FIGURE 9-5** From position  $(x, y)$  on a scan line, the next position across the line has coordinates  $(x + 1, y)$ , and the position immediately below on the next line has coordinates  $(x, y - 1)$ .



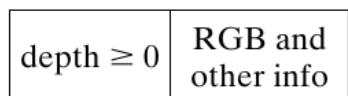
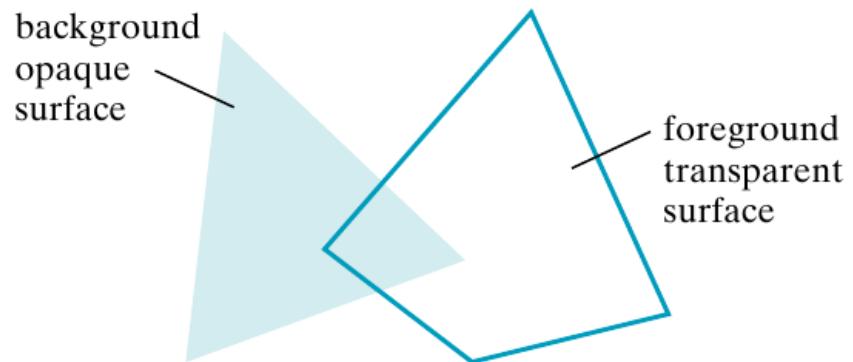
**FIGURE 9-6** Scan lines intersecting a polygon surface.



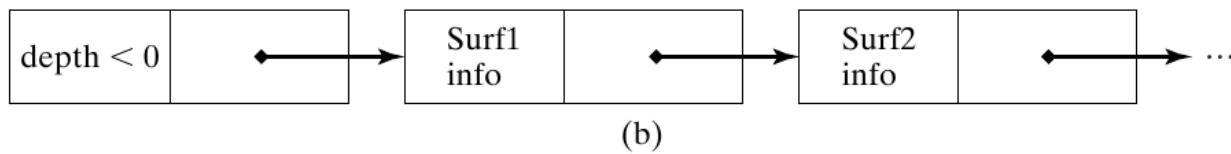
**FIGURE 9-7** Intersection positions on successive scan lines along a left polygon edge.

# Accumulation Buffer

**FIGURE 9-8** Viewing an opaque surface through a transparent surface requires multiple color inputs and the application of color-blending operations.



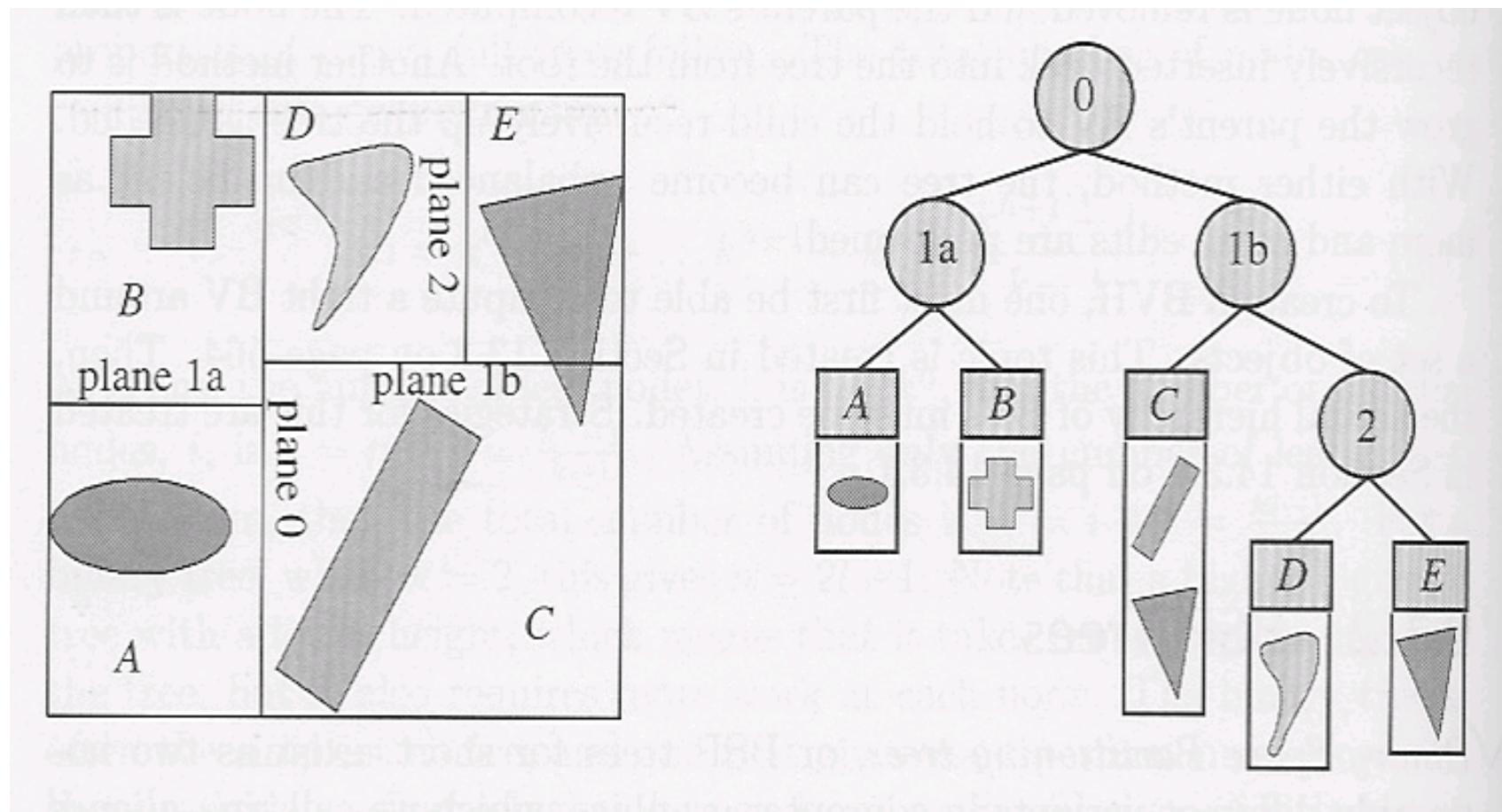
(a)



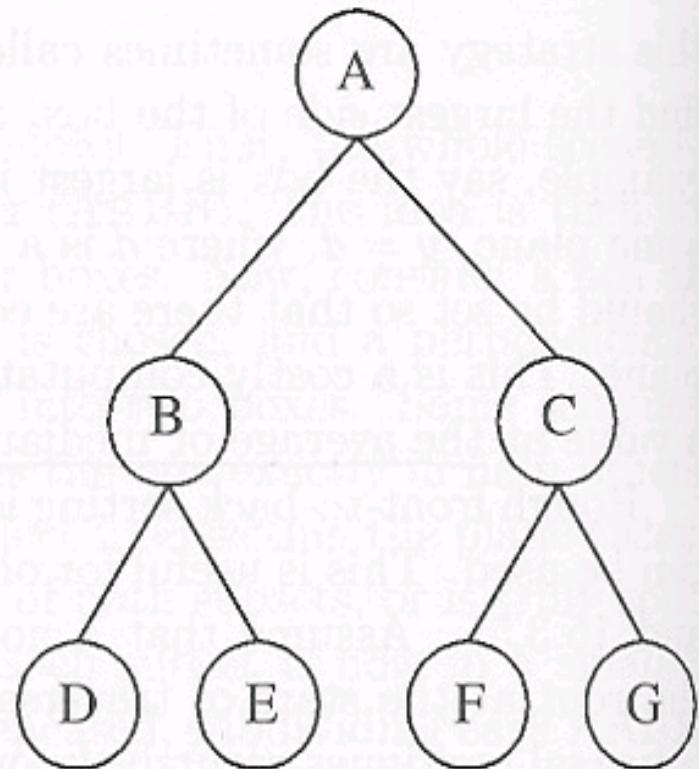
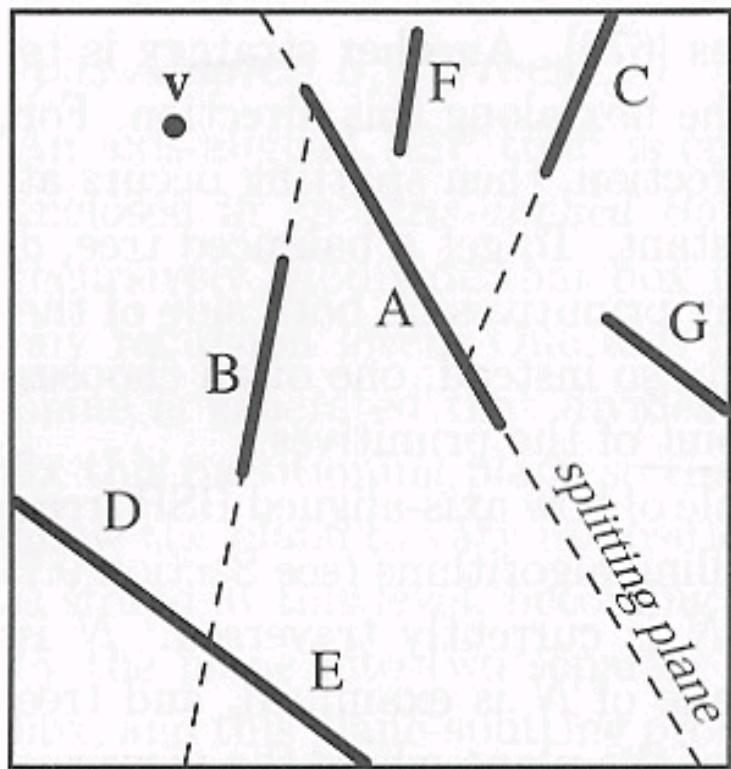
(b)

**FIGURE 9-9** Two possible organizations for surface information in an A-buffer representation for a pixel position. When a single surface overlaps the pixel, the surface depth, color, and other information are stored as in (a). When more than one surface overlaps the pixel, a linked list of surface data is stored as in (b).

# Axis-Parallel BSP Tree

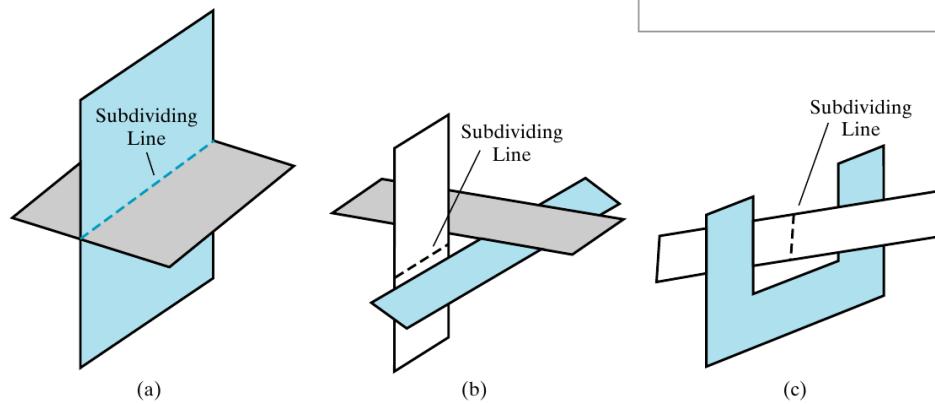
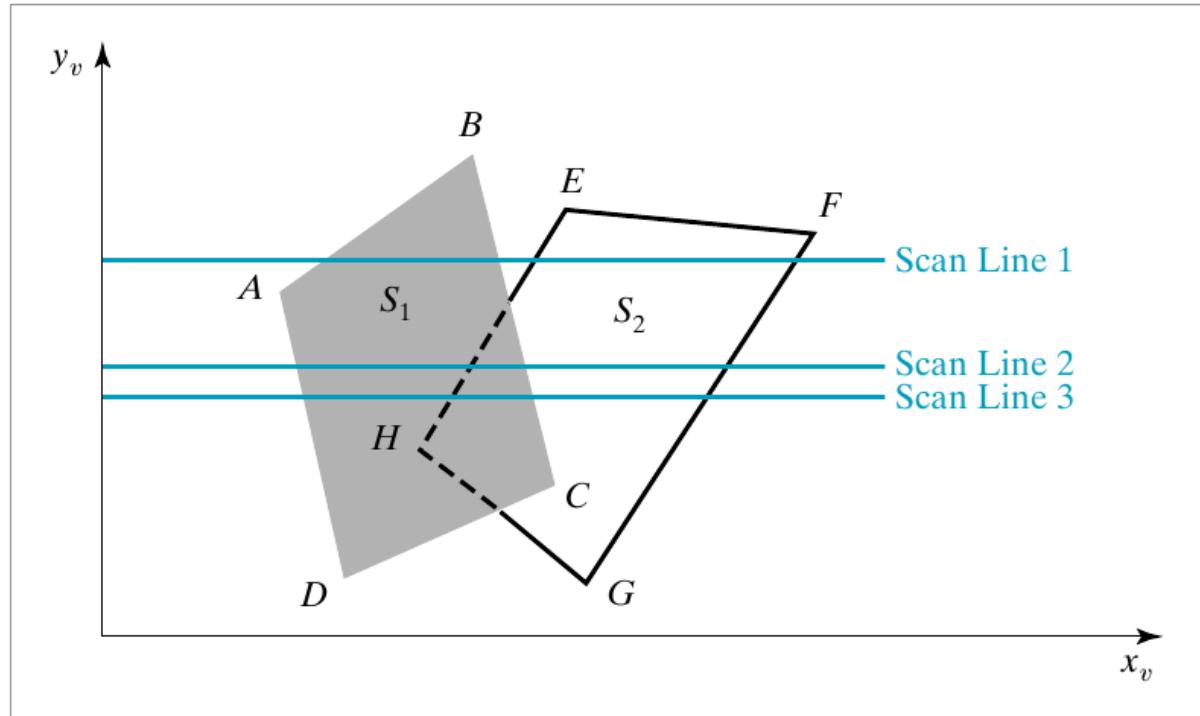


# General BSP Tree



# Scan-Line Method

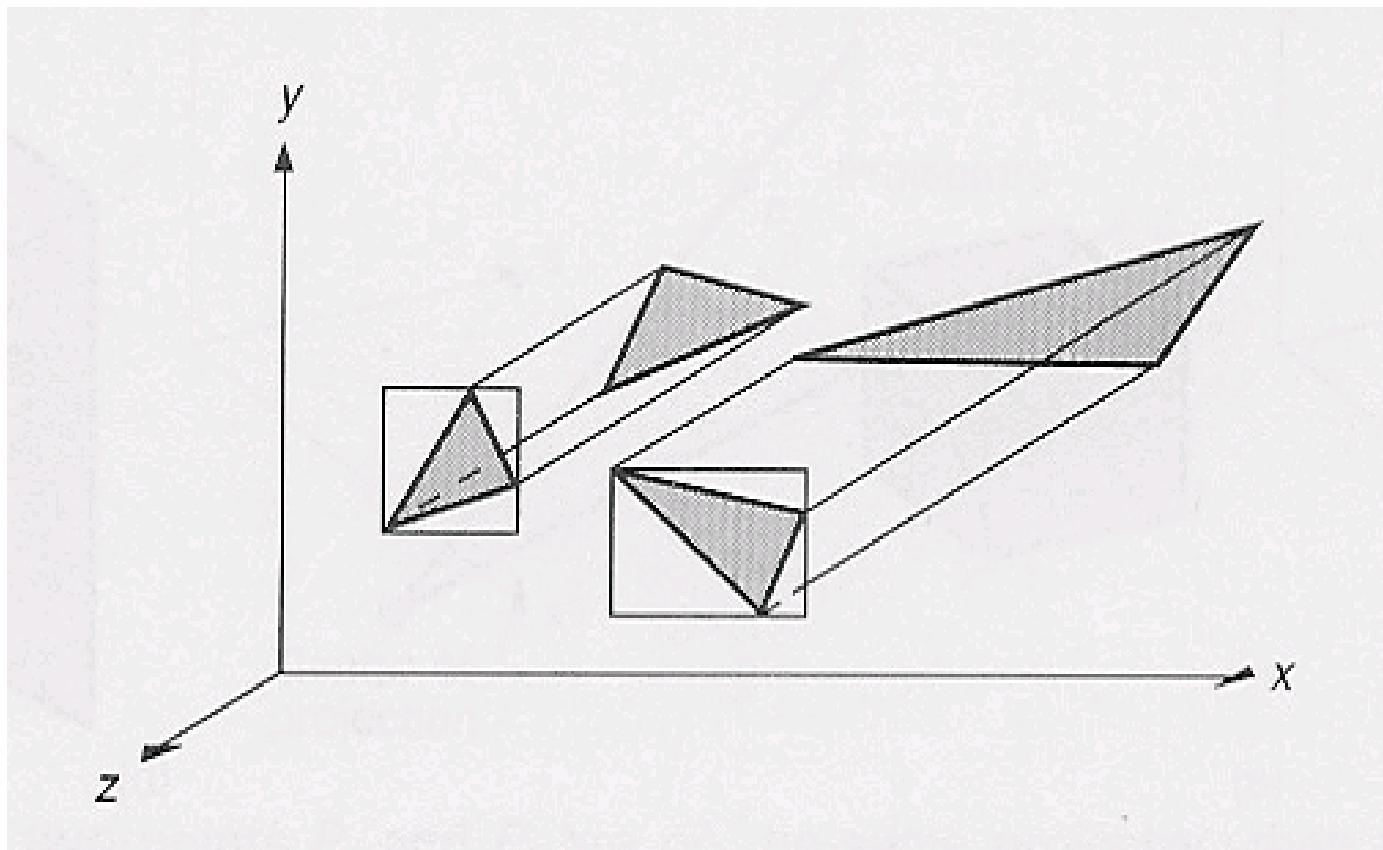
**FIGURE 9-10** Scan lines crossing the view-plane projection of two surfaces,  $S_1$  and  $S_2$ . Dashed lines indicate the boundaries of hidden surface sections.



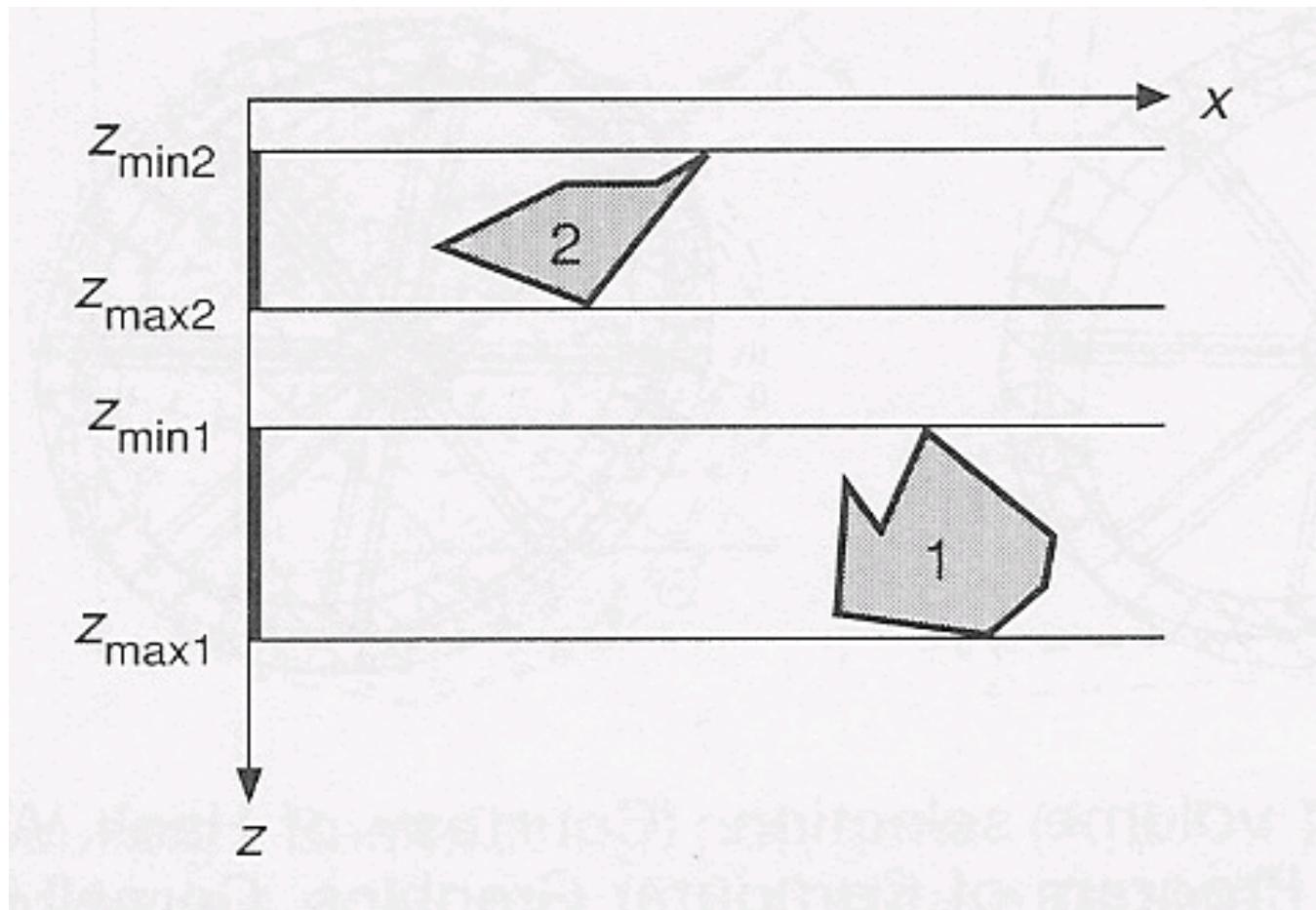
**FIGURE 9-11** Intersecting and cyclically overlapping surfaces that alternately obscure one another.

# Depth-Sorting Method

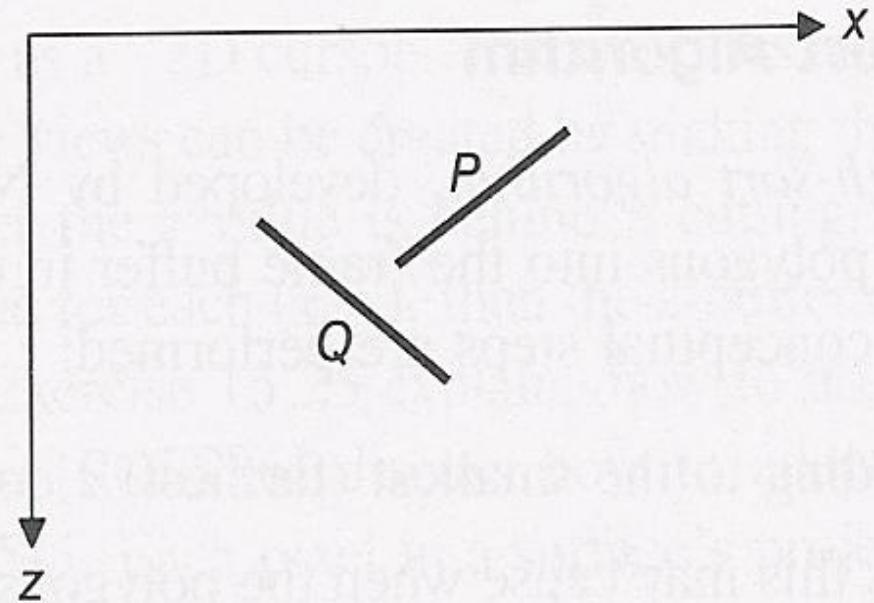
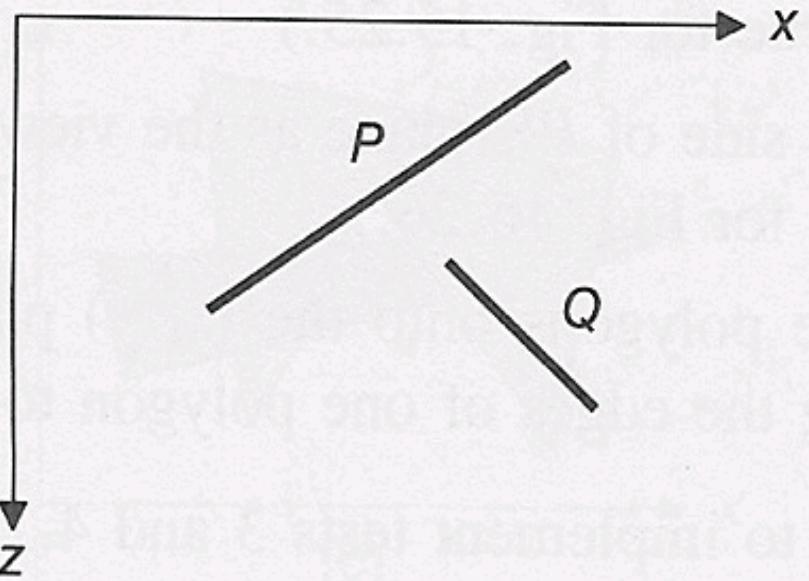
- 투영후 겹치지 않는 경우:  
아무 순서로 그려도 상관 없다.



- 깊이 범위가 다른 경우:  
먼 쪽의 물체를 먼저 가까운 쪽을 나중에.



- 앞뒤 관계가 분명한 경우:  
P를 먼저 그리고, Q를 나중에 그린다.



- 깊이가 겹치는 경우:
  - $Q$ 를 먼저 그리고,  $P$ 를 나중에 그린다.
  - $P$ 를 절단하여 순서를 결정한다.
  - $R$ 을 절단하여 순서를 정한다.

