

Programming #3: Part I (4190.410)

Due: October 7, 2013

A cubic Bézier curve $C(t) = \sum_{l=0}^3 \mathbf{b}_l B_l^3(t)$, $0 \leq t \leq 1$, can be approximated by a polygonal curve $L^h(t)$ connecting a sequence of curve points $C(t_i^h) = C(i/2^h)$, for $i = 0, \dots, 2^h$, within an approximation error bound (Filip et al., CAGD 1986):

$$\|C(t) - L^h(t)\| \leq \frac{3}{4} \cdot \frac{1}{4^h} \cdot \max(\|\mathbf{b}_0 - 2\mathbf{b}_1 + \mathbf{b}_2\|, \|\mathbf{b}_1 - 2\mathbf{b}_2 + \mathbf{b}_3\|) = \epsilon_h.$$

More precisely, each line segment $L_i^h(t)$, $(t_{i-1}^h \leq t \leq t_i^h)$, approximates the corresponding curve segment $C_i^h(t) = C(t)$, $(t_{i-1}^h \leq t \leq t_i^h)$, within the error bound $\epsilon_h \geq 0$.

Design an interactive system that can show the BVH structure (i.e., the AABB tree and the LSS tree) for the Bézier curve $C(t)$. Display the rounded AABB bounding volumes generated by expanding the AABB containing each line segment $L_i^h(t)$ by ϵ_h . Moreover, display the LSS bounding volumes generated by sweeping a disc of radius ϵ_h along each line segment $L_i^h(t)$, for the levels $h = 2, \dots, 10$.