Programming #1 (4190.562) Due: March 28, 2018

A cubic Bézier curve $C(t) = \sum_{l=0}^{3} \mathbf{b}_l B_l^3(t) = \sum_{l=0}^{3} (x_l, y_l) B_l^3(t) = (x(t), y(t)), 0 \le t \le 1$, can be used to define a different planar curve D(t) as follows:

 $D(t) = C(t) + \alpha(\sin n\pi t) C'(t)^{\perp}, \quad 0 \le t \le 1,$

where α is a scale factor, and n is a natural number. When we edit the curve C(t), the other curve D(t) also changes its shape. Compute the self-intersection points of D(t), $0 \le t \le 1$.