Quiz #2 (CSE 4190.313)

Monday, March 30, 2015

 Name:
 ID No:

1. (10 points) Given an $m \times n$ matrix A with rank r, if you know a particular solution \mathbf{x}_p (free variables = 0) and all special solutions $\mathbf{x}_1, \dots, \mathbf{x}_{n-r}$, for

 $A\mathbf{x} = \mathbf{b},$

(a) (2 points) Find a solution \mathbf{y}_p and all special solutions $\mathbf{y}_1, \cdots, \mathbf{y}_{n-r}$, for

$$A\mathbf{y} = 2\mathbf{b}.$$

(b) (3 points) Find a solution \mathbf{y}_p and all special solutions $\mathbf{y}_1, \dots, \mathbf{y}_{n-r}$, for

$$\begin{bmatrix} A \\ A \end{bmatrix} \begin{bmatrix} \mathbf{y} \end{bmatrix} = \begin{bmatrix} \mathbf{b} \\ \mathbf{b} \end{bmatrix}.$$
(c) (5 points) Find a solution $\begin{bmatrix} \mathbf{y}_p \\ \mathbf{Y}_p \end{bmatrix}$ and all special solutions $\begin{bmatrix} \mathbf{y}_1 \\ \mathbf{Y}_1 \end{bmatrix}, \cdots, \begin{bmatrix} \mathbf{y}_{2n-r} \\ \mathbf{Y}_{2n-r} \end{bmatrix},$
for
$$\begin{bmatrix} A & A \end{bmatrix} \begin{bmatrix} \mathbf{y} \\ \mathbf{Y} \end{bmatrix} = \mathbf{b}.$$

- 2. (6 points) (True or False) For the vector space M of all 3×3 matrices, justify your answer for the following problems:
 - (a) (2 points) The skew-symmetric matrices in M (with $A^T = -A$) form a subspace.
 - (b) (2 points) The unsymmetric matrices in M (with $A^T \neq A$) form a subspace.
 - (c) (2 points) The matrices that have (1, 1, 1) in their nullspace form a subspace.

3. (6 points) Apply elimination with an extra column to reach $R\mathbf{x} = \mathbf{0}$ and $R\mathbf{x} = \mathbf{d}$:

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	U	0	=	0	0	2	0	and	U	с	=	0	0	2	4
	-			0	0	0	0	and	L	_		0	0	0	0

Solve $R\mathbf{x} = \mathbf{0}$ (free variable = 1). What are the solutions to $R\mathbf{x} = \mathbf{d}$?

4. (10 points) Construct a matrix with the required property, or explain why you can't.

