1. (3 points) Compute the following integral using the Gauss quadrature with $n=3$.

$$
\int_{1}^{5} \frac{1}{1+x^{2}} d x
$$

2. (7 points) Interpolate

$$
f_{0}=f(0)=-1, f_{1}=f(1)=3, f_{2}=f(2)=7, \quad f_{3}=f(3)=7
$$

by the cubic spline satisfying $k_{0}=-1$ and $k_{3}=2$.
3. (5 points) If $B$ has the columns of $A$ in reverse order, show that $A-B$ is not invertible.
4. (15 points)
(a) (5 points) For any permutation $P$, show that $P^{k}=I$, for some $k \in\{1,2,3, \cdots\}$.
(b) (10 points) Find a $5 \times 5$ permutation $P$ such that $P^{6}=I$, but $P^{k} \neq I$, for $k=$ $1,2,3,4,5$.

